

13.3 Trig Functions of General Angles HW Day 1

Key

Find the exact values of the 6 trig functions of θ if the terminal side in standard position contains the given point.

1. (7, 24)

$$\sin \theta = \frac{24}{25}$$

$$\cos \theta = \frac{7}{25}$$

$$\tan \theta = \frac{24}{7}$$

$$\csc \theta = \frac{25}{24}$$

$$\sec \theta = \frac{25}{7}$$

$$\cot \theta = \frac{7}{24}$$

2. (2, 1)

$$\sin \theta = \frac{\sqrt{5}}{5}$$

$$\cos \theta = \frac{2\sqrt{5}}{5}$$

$$\tan \theta = \frac{1}{2}$$

$$\csc \theta = \sqrt{5}$$

$$\sec \theta = \frac{\sqrt{5}}{2}$$

$$\tan \theta = 2$$

3. (5, -8)

$$\sin \theta = -\frac{8\sqrt{89}}{89}$$

$$\cos \theta = \frac{5\sqrt{89}}{89}$$

$$\tan \theta = -\frac{8}{5}$$

$$\csc \theta = -\frac{\sqrt{89}}{8}$$

$$\sec \theta = \frac{\sqrt{89}}{5}$$

$$\cot \theta = -\frac{5}{8}$$

4. (4, -3)

$$\sin \theta = -\frac{3}{5}$$

$$\cos \theta = \frac{4}{5}$$

$$\tan \theta = -\frac{3}{4}$$

$$\csc \theta = -\frac{5}{3}$$

$$\sec \theta = \frac{5}{4}$$

$$\cot \theta = -\frac{4}{3}$$

5. (0, -6)

$$\sin \theta = -1$$

$$\cos \theta = 0$$

$$\tan \theta = \text{und.}$$

$$\csc \theta = -1$$

$$\sec \theta = \text{und.}$$

$$\cot \theta = 0$$

6. (-1, 0)

$$\sin \theta = 0$$

$$\cos \theta = -1$$

$$\tan \theta = 0$$

$$\csc \theta = \text{und.}$$

$$\sec \theta = -1$$

$$\cot \theta = \text{und.}$$

7. ($\sqrt{2}, -\sqrt{2}$)

$$\sin \theta = -\frac{\sqrt{2}}{2}$$

$$\cos \theta = \frac{\sqrt{2}}{2}$$

$$\tan \theta = -1$$

$$\csc \theta = -\sqrt{2}$$

$$\sec \theta = \sqrt{2}$$

$$\cot \theta = -1$$

8. (- $\sqrt{3}, -\sqrt{6}$)

$$\sin \theta = -\frac{\sqrt{6}}{3}$$

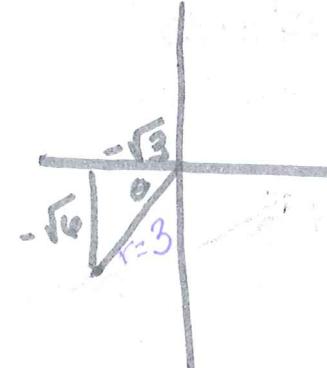
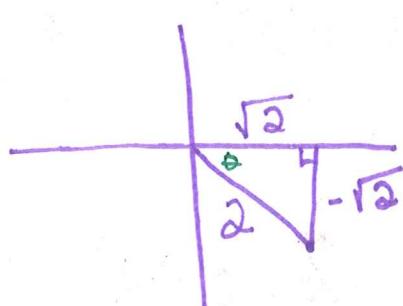
$$\cos \theta = -\frac{\sqrt{3}}{3}$$

$$\tan \theta = \sqrt{2}$$

$$\csc \theta = -\frac{\sqrt{6}}{2}$$

$$\sec \theta = -\sqrt{3}$$

$$\cot \theta = \frac{\sqrt{2}}{2}$$

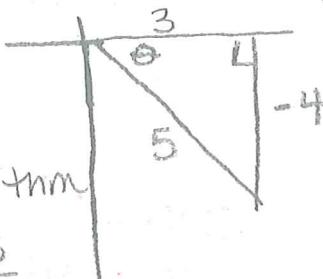


Suppose θ is an angle in standard position whose terminal side is in the given quadrant. For each function, find the exact values of the remaining five trig functions.

9. $\cos \theta = \frac{3}{5}$, Quadrant IV

$$x=3 \quad y=-4 \quad r=5$$

pyth. thm



$$\sin \theta = -\frac{4}{5}$$

$$\csc \theta = -\frac{5}{4}$$

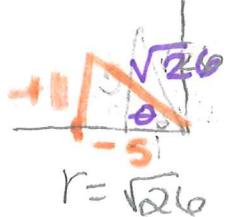
$$\tan \theta = -\frac{4}{3}$$

$$\sec \theta = \frac{5}{3}$$

$$\cot \theta = -\frac{3}{5}$$

~~$x=-5 \quad y=1$~~

10. $\tan \theta = -\frac{1}{5}$, Quadrant II



$$r = \sqrt{26}$$

$$\sin \theta = \frac{+\sqrt{26}}{26}$$

$$\cos \theta = -\frac{5\sqrt{26}}{26}$$

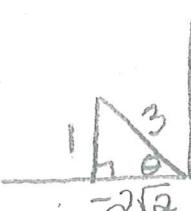
$$\csc \theta = \sqrt{26}$$

$$\sec \theta = -\frac{\sqrt{26}}{5}$$

$$\cot \theta = -5$$

11. $\sin \theta = \frac{1}{3}$, Quadrant II

$$x = -2\sqrt{2}, \quad y = 1 \quad r = 3$$



$$\sin \theta = \frac{1}{3}$$

$$\csc \theta = 3$$

$$\cos \theta = -\frac{2\sqrt{2}}{3}$$

$$\sec \theta = \frac{3}{-2\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{-3\sqrt{2}}{2\sqrt{4}} = \frac{-3\sqrt{2}}{4}$$

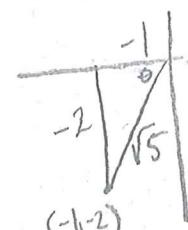
$$\sec \theta = -\frac{3\sqrt{2}}{4}$$

$$\cot \theta = -2\sqrt{2}$$

12. $\cot \theta = -\frac{1}{2}$, Quadrant III

$$\frac{x}{4} = -\frac{1}{2} \quad x = -1$$

$$y = -2$$



$$\sin \theta = -\frac{2\sqrt{5}}{5}$$

$$\cos \theta = -\frac{\sqrt{5}}{5}$$

$$\csc \theta = -\frac{\sqrt{5}}{2}$$

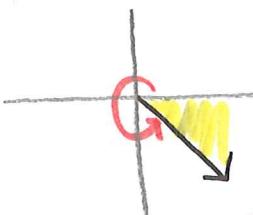
$$\tan \theta = 2$$

$$\sec \theta = -\sqrt{5}$$

Review:

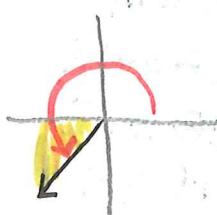
Sketch each angle. Then find its reference angle.

34. 315°



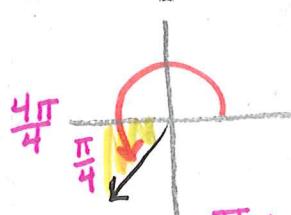
$$\theta' = 45^\circ$$

35. 240°



$$\theta' = 60^\circ$$

36. $\frac{5\pi}{4}$



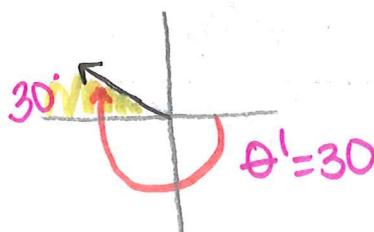
$$\theta' = \pi/4$$

37. $\frac{5\pi}{6}$



$$\theta' = \pi/6$$

38. -210°



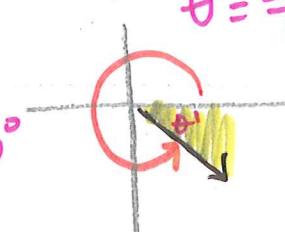
$$\theta' = 30^\circ$$

39. -125°



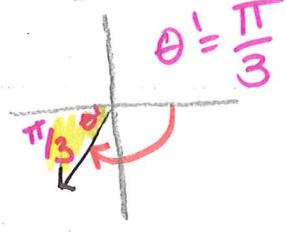
$$\theta' = 55^\circ$$

40. $\frac{13\pi}{7}$



$$\theta' = \pi/7$$

41. $-\frac{2\pi}{3}$



$$\theta' = \pi/3$$