

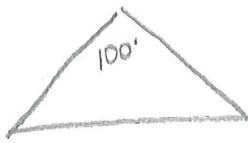
## Section 4.1 & 4.2 Triangle Basics

A triangle can be classified by its Sides and Angles.

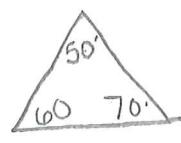
Angle Classification:



right

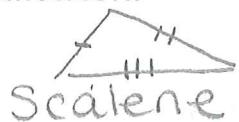


obtuse



acute

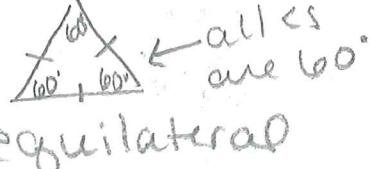
Side Classification:



scalene



isosceles



equilateral

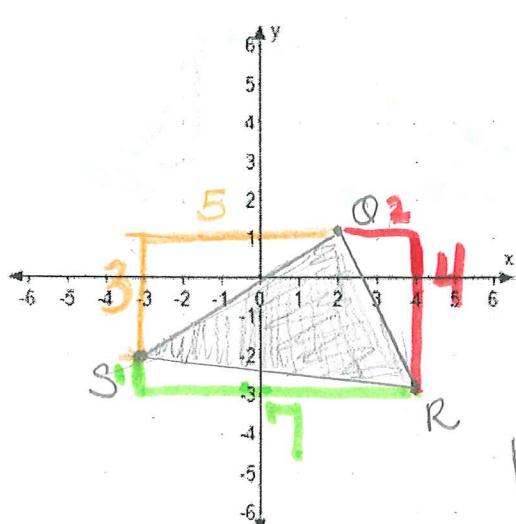
Example 1: Find  $d$  and the measure of each side of equilateral triangle  $KLM$ .  $KL = d+2$ ,  $LM = 12-d$ , and  $KM = 4d-13$ .

$$\begin{aligned} KL &= LM \\ d+2 &= 12-d \\ 2d &= 10 \\ d &= 5 \end{aligned}$$

def of  
equilateral  $\Delta$

$$\begin{aligned} KL &= 7 \\ LM &= 7 \\ KM &= 7 \end{aligned}$$

Example 2: Find the measures of the sides of triangle  $QRS$  with  $Q(2,1)$ ,  $R(4,-3)$  and  $S(-3,-2)$ . Classify the triangle.



$$SQ = \sqrt{3^2 + 5^2} = \sqrt{34}$$

$$QR = \sqrt{2^2 + 4^2} = \sqrt{20} = 2\sqrt{5}$$

$$SR = \sqrt{1^2 + 7^2} = \sqrt{50} = 5\sqrt{2}$$

Scalene

Is  $Q$  a right angle? No...  
Why?

Check if slopes are  $\perp$

Slope  $SQ: \frac{3}{5}$   $\rightarrow$  NOT  $\perp$

Slope  $QR: -\frac{4}{2} = -2$

## The Triangle Sum Theorem states

the interior angles of  
a triangle add to  $= 180^\circ$

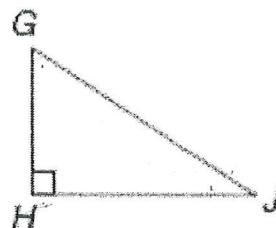
Corollary: The angles of a right triangle are complementary.

Proof:

Given:  $\triangle GHJ$  is a right triangle.

Prove:  $\angle G + \angle H = 90^\circ$

$\angle J$



1.  $\triangle GHJ$  is a RT $\Delta$

2.  $\angle H = 90^\circ$

3.  $\angle G + \angle J + \angle H = 180^\circ$

4.  $\angle G + \angle J + 90^\circ = 180^\circ$

5.  $\angle G + \angle J = 90^\circ$

1. given

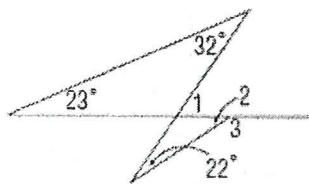
2. def of Right  $\Delta$

3.  $\Delta$  sum thm.

4. substitution

5. Subtraction

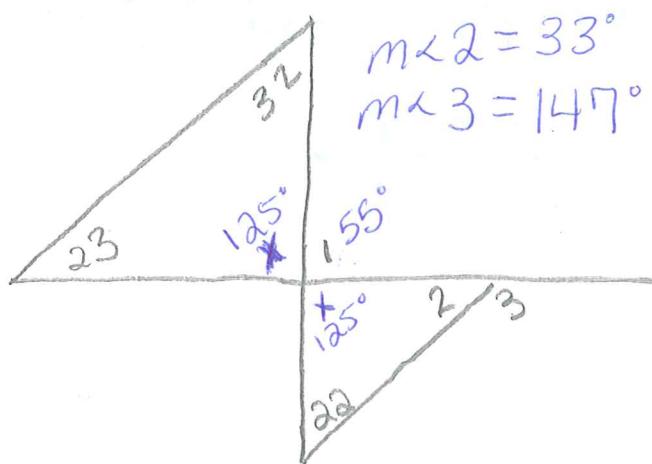
Example 3: Find each missing measure.



$$m\angle 1 = 55^\circ$$

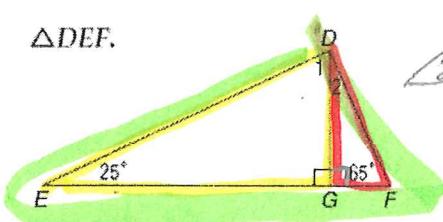
$$m\angle 2 = 33^\circ$$

$$m\angle 3 = 147^\circ$$



Example 4: Find each missing measure.

$\triangle DEF$ .



$$\begin{aligned} m\angle 1 &= 65^\circ \\ m\angle 2 &= 25^\circ \end{aligned}$$

