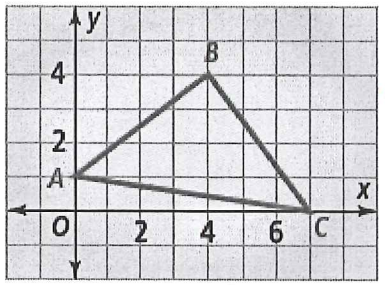


Triangle Coordinate Geometry Examples Day 1

1. Classify the triangle as scalene, equilateral, or isosceles. Then determine if the triangle is a right triangle.



Work:

$$3^2 + 4^2 = AB^2$$

$$9 + 16 = AB^2$$

$$\sqrt{25} = AB$$

$$5 = AB$$

$$3^2 + 4^2 = BC^2$$

$$5 = BC$$

$AB \cong BC$

$$1^2 + 7^2 = AC^2$$

$$50 = AC^2$$

$$\sqrt{50} = AC$$

$$5\sqrt{2} = AC$$

$\sqrt{50} = \sqrt{25 \cdot 2} = 5\sqrt{2}$

Slope AB = $\frac{3}{4}$

Slope BC = $-\frac{4}{3}$

Slope AC = $-\frac{1}{7}$

$AB \perp BC!!$

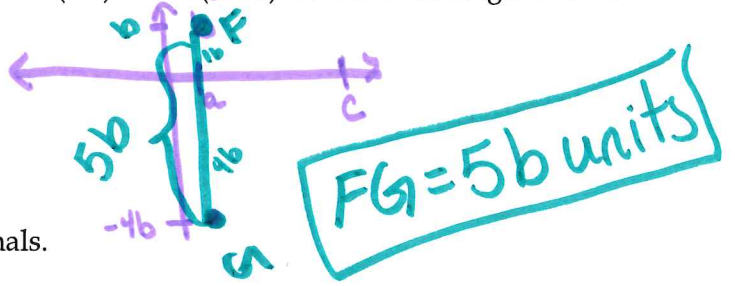
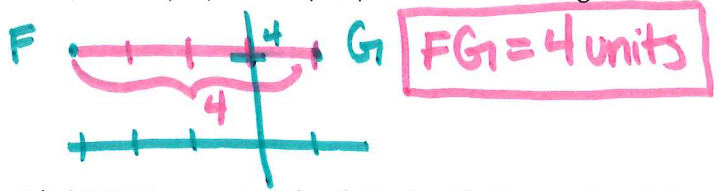
Conclude:

$AB \cong BC \therefore \triangle ABC$ is an isosceles \triangle .

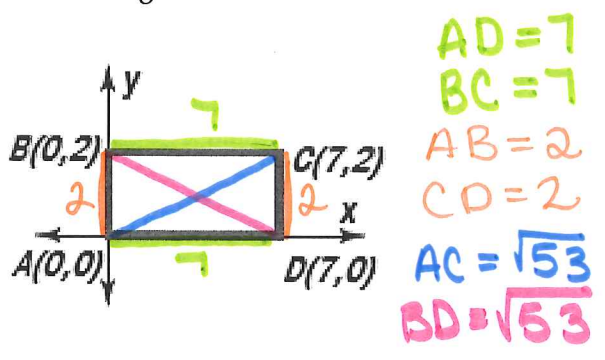
$AB \perp BC \therefore \triangle ABC$ is a Right \triangle

$\triangle ABC$ is a Right Isosceles Triangle!

2. a.) Plot F(1,4) and G(-3,4). What is the length of FG? b.) Plot F(a,b) and G(c,-4b). What is the length of FG?



3.) ABCD is a rectangle plotted with the vertices below.
a.) Find the lengths of ALL FOUR SIDES and BOTH Diagonals.



Find AC

$$7^2 + 2^2 = x^2$$

$$49 + 4 = x^2$$

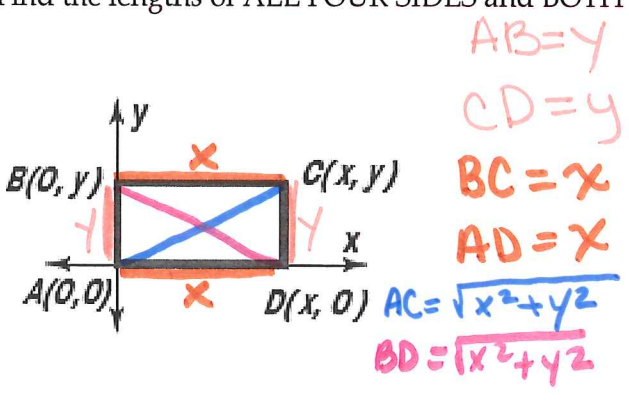
$$\sqrt{53} = x$$

Find BD

$$7^2 + 2^2 = BD^2$$

$$\sqrt{53} = BD$$

ABCD is a rectangle plotted with the vertices below.
b.) Find the lengths of ALL FOUR SIDES and BOTH Diagonals.



Find AC

$$x^2 + y^2 = AC^2$$

$$\sqrt{x^2 + y^2} = AC$$

Find BD

$$x^2 + y^2 = BD^2$$

$$\sqrt{x^2 + y^2} = BD$$

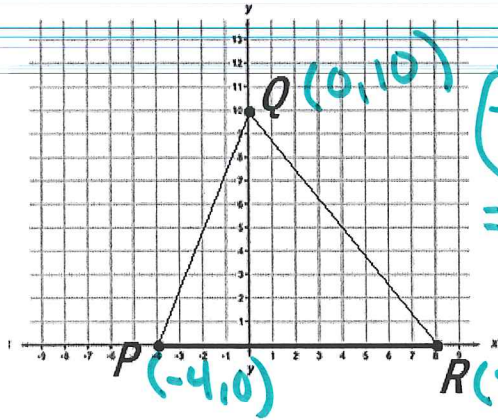
Can't CLT so leave as is take $\sqrt{\quad}$

4. M and N are midpoints of QP and QR respectively for ΔPQR . $P(-4,0)$, $Q(0,10)$, and $R(8,0)$.

a.) Find the coordinates of midpoints M and N. To check midpoints, use the midpoint formula.

midpoint

Formula



Find M

$$\left(\frac{-4+0}{2}, \frac{0+10}{2} \right) = \left(-\frac{4}{2}, \frac{10}{2} \right) = \boxed{M(-2,5)}$$

Find N:

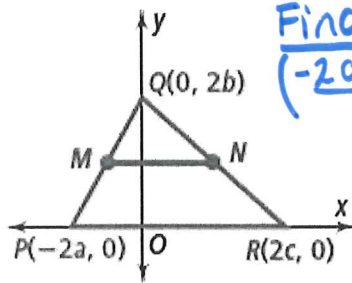
$$\left(\frac{8+0}{2}, \frac{0+10}{2} \right) = \left(\frac{8}{2}, \frac{10}{2} \right) = N(4,5)$$

$$\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right)$$

M: $\underline{(-2,5)}$ N: $\underline{(4,5)}$

b.) M and N are midpoints of QP and QR respectively.

Find the coordinates of midpoints M and N. To check midpoints, use the midpoint formula.



Find M

$$\left(\frac{-2a+0}{2}, \frac{0+2b}{2} \right) = \left(-\frac{2a}{2}, \frac{2b}{2} \right) = \boxed{M(-a,b)}$$

Find N:

$$\left(\frac{2c+0}{2}, \frac{0+2b}{2} \right) = \left(\frac{2c}{2}, \frac{2b}{2} \right) = N(c,b)$$

$$= N(c,b)$$

M: $\underline{(-a,b)}$ N: $\underline{(c,b)}$

5. M and N are midpoints of QP and QR respectively for ΔPQR . $P(-4,0)$, $Q(0,10)$, and $R(8,0)$. Record your midpoints from the previous question.

a.) Is $MN \parallel PR$? Why or why not. SHOW MATH! To check parallel, we need to look at slopes!

Some slopes mean parallel lines!

Slope PR = $\frac{0-0}{-4-8} = \frac{0}{-12} = 0$

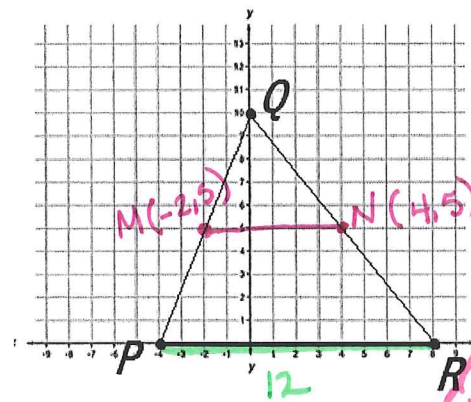
$\boxed{\text{Slope PR} = 0}$

Slope MN = $\frac{5-5}{-2-4} = \frac{0}{-6} = 0$

$\boxed{\text{Slope MN} = 0}$

slope PR and slope MN are the same so $MN \parallel PR$

Slope formula!
 $\frac{y_2 - y_1}{x_2 - x_1} = \frac{\text{rise}}{\text{run}}$



b.) Record your midpoints from the previous question. Is $MN \parallel PR$? Why or why not. SHOW MATH! To check parallel, we need to look at slopes!

Formula s:

Slope MN = $\frac{b-b}{-a-c} = \frac{0}{-a-c} = 0$

Slope PR = $\frac{0-0}{2a-2c} = \frac{0}{2a-2c} = 0$

$\boxed{\text{Slope PR} = 0}$

same slopes $\therefore MN \parallel PR$

Rise/run

Slope MN = $\frac{0}{a+c} = 0$

$\boxed{\text{Slope MN} = 0}$

Slope PR = $\frac{0}{2a+2c} = 0$

$\boxed{\text{Slope PR} = 0}$

