

Day one

Name: _____

Hour: _____

Coordinate Proofs of Congruent Triangles

1. Given: the Coordinates of Square ABCD

Prove: $\triangle ABC \cong \triangle ADC$

$$AD = a$$

$$DC = a$$

$$AC^2 = a^2 + a^2$$

$$AC^2 = 2a^2$$

$$AC = a\sqrt{2}$$

$$AB = a$$

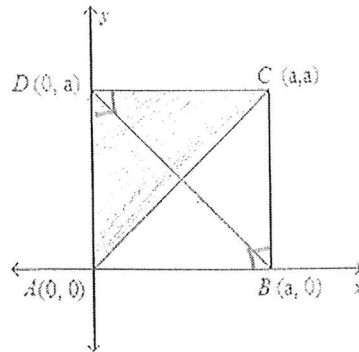
$$BC = a$$

$$AC \cong AC \text{ reflexive}$$

$$AD \cong AB$$

$$DC \cong BC$$

$$\triangle ABC \cong \triangle ADC \text{ by SSS}$$



2. Given: the Coordinates of Square ABCD

Prove: $AC \cong BD$

$$AC^2 = a^2 + a^2$$

$$\sqrt{AC^2} = \sqrt{2a^2}$$

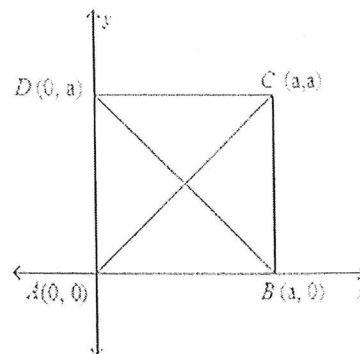
$$AC = a\sqrt{2}$$

$$BD^2 = a^2 + a^2$$

$$\sqrt{BD^2} = \sqrt{2a^2}$$

$$BD = a\sqrt{2}$$

$$AC \cong BD$$



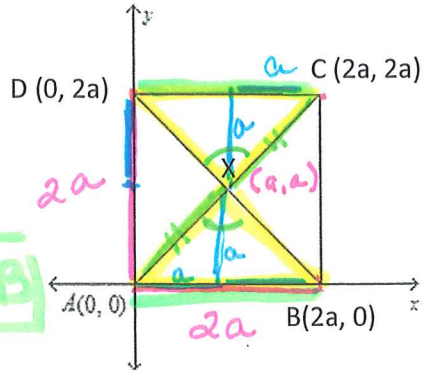
3. Given: the Coordinates of Square ABCD

Prove: $\triangle ABX \cong \triangle CDX$

How could we prove by SSS?

$DC = 2a$
 $AB = 2a$

$DC \cong AB$



$a^2 + a^2 = AX^2$

$a^2 + a^2 = CX^2$

$2a^2 = AX^2$

$CX = a\sqrt{2}$

$AX = a\sqrt{2}$

$AX \cong CX$ Side

\therefore by SAS
 $\triangle ABX \cong \triangle CDX$

Angle $\angle CXD \cong \angle AXB$ vertical \angle s are \cong

$a\sqrt{2} = DX$

$a\sqrt{2} = BX$

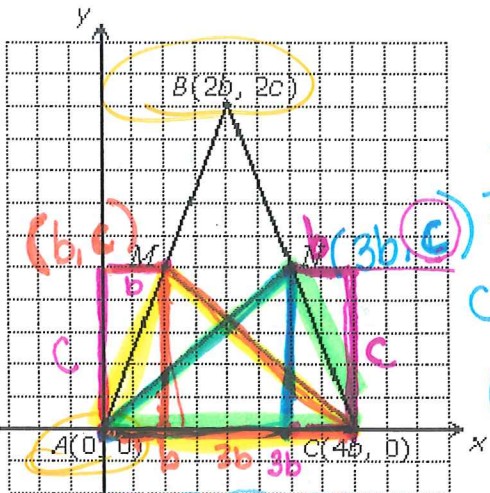
$BX \cong DX$
Side

4. Given $A(0,0)$, $B(2b,2c)$ and $C(4b,0)$ and M and N are the midpoints of AB and BC respectively.

Prove: $\triangle MCA \cong \triangle NAC$

midpoint formula

$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$



To Find N

$B(2b, 2c)$

$C(4b, 0)$

$\left(\frac{2b + 4b}{2}, \frac{2c + 0}{2} \right)$

$\left(\frac{6b}{2}, \frac{2c}{2} \right) = N(3b, c)$

Find M

$A(0,0)$ $B(2b, 2c)$

$\left(\frac{0 + 2b}{2}, \frac{0 + 2c}{2} \right)$

$\left(\frac{2b}{2}, \frac{2c}{2} \right) =$

$M(b, c)$

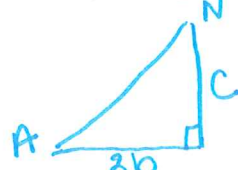
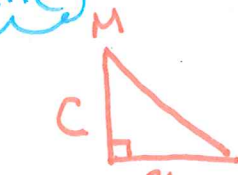
$AC \cong AC$ by Reflexive

$b^2 + c^2 = MC^2$

$\sqrt{b^2 + c^2} = MC$

$b^2 + c^2 = MA^2$

$\sqrt{b^2 + c^2} = MA$



$(3b)^2 + c^2 = MC^2$

$\sqrt{9b^2 + c^2} = MC$

$MC = \sqrt{9b^2 + c^2}$

$(3b)^2 + c^2 = AN^2$

$9b^2 + c^2 = AN^2$

$AN = \sqrt{9b^2 + c^2}$

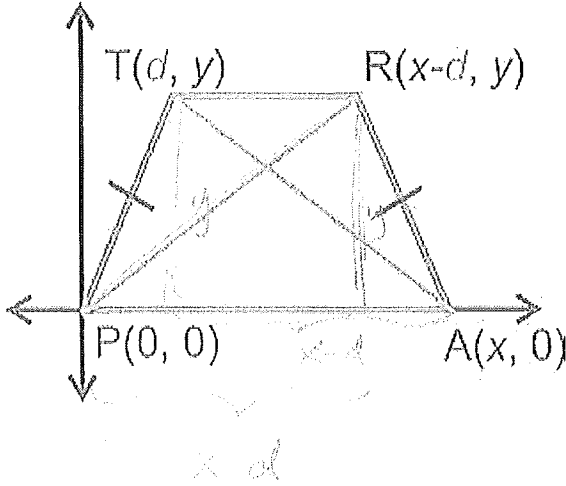
$MC \cong NA$

$\triangle MCA \cong \triangle NAC$ by SSS



7. Given: the coordinates of figure PTRA

Prove: $\triangle PTR \cong \triangle ART$



$$PR^2 = (x-d)^2 + y^2$$

$$PR = \sqrt{(x-d)^2 + y^2}$$

$$TA^2 = (x-d)^2 + y^2$$

$$TA = \sqrt{(x-d)^2 + y^2}$$

$$PR \cong TA$$

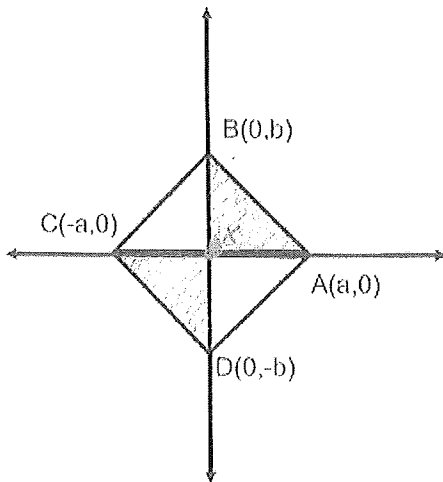
$$TR \cong TR \text{ Reflexive}$$

$$TP \cong RA \text{ Given}$$

SSS

8. Given: the coordinates of $\triangle AXB$ and $\triangle CXD$

Prove: $\triangle AXB \cong \triangle CXD$



$$XB = b$$

$$XD = b$$

$$XB \cong XD$$

$$XA = a$$

$$XC = a$$

$$XA \cong XC$$

$$AB^2 = a^2 + b^2$$

$$CD^2 = a^2 + b^2$$

$$AB = \sqrt{a^2 + b^2}$$

$$CD = \sqrt{a^2 + b^2}$$

$$AB \cong CD$$

$\triangle AXB \cong \triangle CXD$ by SSS

3. Given: the Coordinates of Square ABCD

Prove: $\triangle ABX \cong \triangle CDX$

$$\left. \begin{array}{l} AB = 2a \\ DC = 2a \end{array} \right\} AB \cong DC$$

$$AX^2 = a^2 + a^2 \quad BX^2 = a^2 + a^2$$

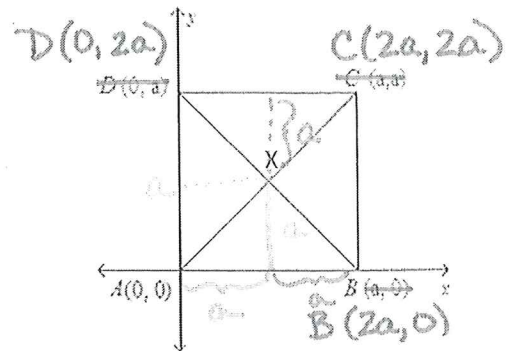
$$AX = a\sqrt{2} \quad BX = a\sqrt{2}$$

$$XD^2 = a^2 + a^2 \quad XC^2 = a^2 + a^2$$

$$XD = a\sqrt{2} \quad XC = a\sqrt{2}$$

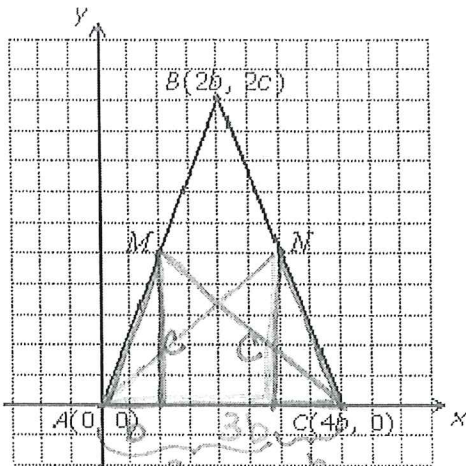
$$\begin{array}{l} AX \cong XD \\ BX \cong XC \end{array}$$

$\triangle ABX \cong \triangle CDX$
by SSS



4. Given $A(0,0)$, $B(2b,2c)$ and $C(4b,0)$ and M and N are the midpoints of AB and BC respectively.

Prove: $\triangle MCA \cong \triangle NAC$



$$M = \left(\frac{0+2b}{2}, \frac{0+2c}{2} \right) = (b, c)$$

$$N = \left(\frac{2b+4b}{2}, \frac{2c+0}{2} \right) = (3b, c)$$

$AC \cong AC$ reflexive

$$\sqrt{MA^2} = \sqrt{b^2 + c^2}$$

$$\sqrt{MC^2} = \sqrt{3b^2 + c^2}$$

$$MA \cong NC$$

$$MA = \sqrt{b^2 + c^2}$$

$$MC = \sqrt{3b^2 + c^2}$$

$$MC \cong AN$$

$$\sqrt{NC^2} = \sqrt{b^2 + c^2}$$

$$\sqrt{AN^2} = \sqrt{3b^2 + c^2}$$

$\triangle MCA \cong \triangle NAC$ by SSS

$$NC = \sqrt{b^2 + c^2}$$

$$AN = \sqrt{3b^2 + c^2}$$