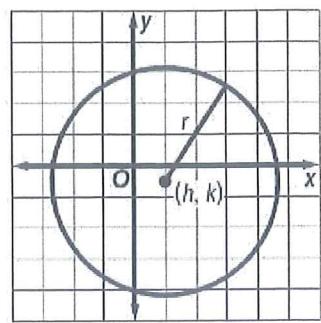


## 10-8 Equations of Circles: Notes

**Equation of a Circle** A circle is the locus of points in a plane equidistant from a given point. You can use this definition to write an equation of a circle.

**Standard Equation of a Circle** An equation for a circle with center at  $(h, k)$  and a radius of  $r$  units is  $(x - h)^2 + (y - k)^2 = r^2$ .



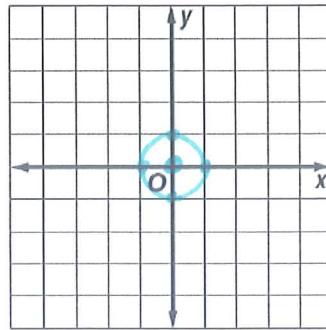
Write the equation for each circle, then graph each.

ex1. Center at  $(0, 0)$ ,  $r=1$  *Plug in!*

$$(x-h)^2 + (y-k)^2 = r^2$$

$$(x-0)^2 + (y-0)^2 = 1^2$$

$$\boxed{x^2 + y^2 = 1}$$

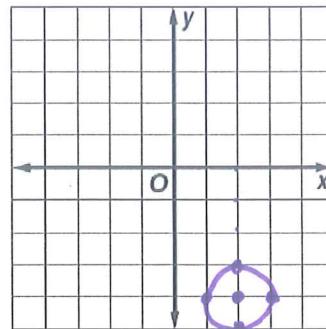


ex2. Center at  $(2, -4)$ ,  $r = 1$  *Watch negative!*

$$(x-h)^2 + (y-k)^2 = r^2$$

$$(x-2)^2 + (y-(-4))^2 = 1^2$$

$$\boxed{(x-2)^2 + (y+4)^2 = 1}$$

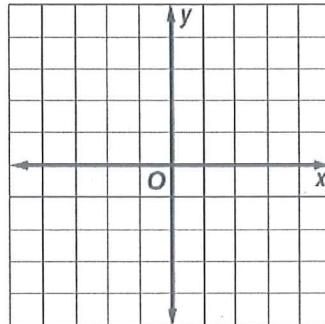


ex3. Center at  $(4, 3)$ ,  $r = 9$

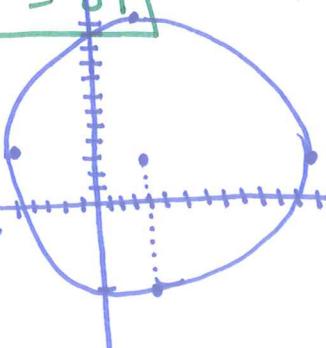
$$(x-h)^2 + (y-k)^2 = r^2$$

$$(x-4)^2 + (y-3)^2 = 9^2$$

$$\boxed{(x-4)^2 + (y-3)^2 = 81}$$

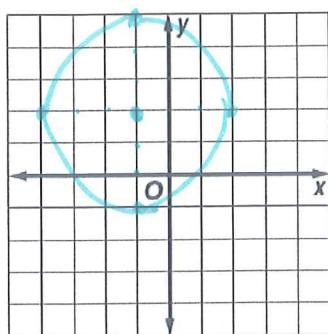


On SAT and exams also  
Alg 2 you  
need to be able  
to make own  
grid.



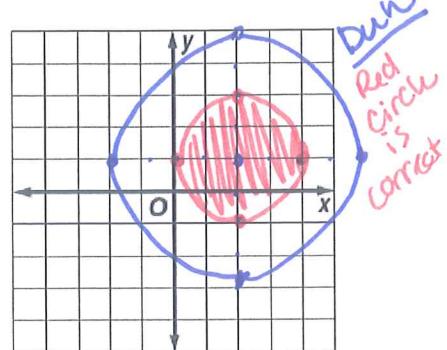
Find the center and the radius and graph each equation.

Ex 4.  $(x + 1)^2 + (y - 2)^2 = 9$



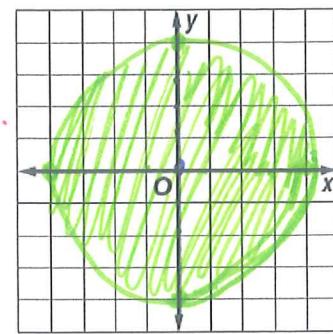
Center:  $(-1, 2)$

Ex 5.  $(x - 2)^2 + (y - 1)^2 = 4$



Center:  $(2, 1)$

Ex 6.  $x^2 + y^2 = 16$



Center:  $(0, 0)$

$$r = \sqrt{9}$$

$r = 3$

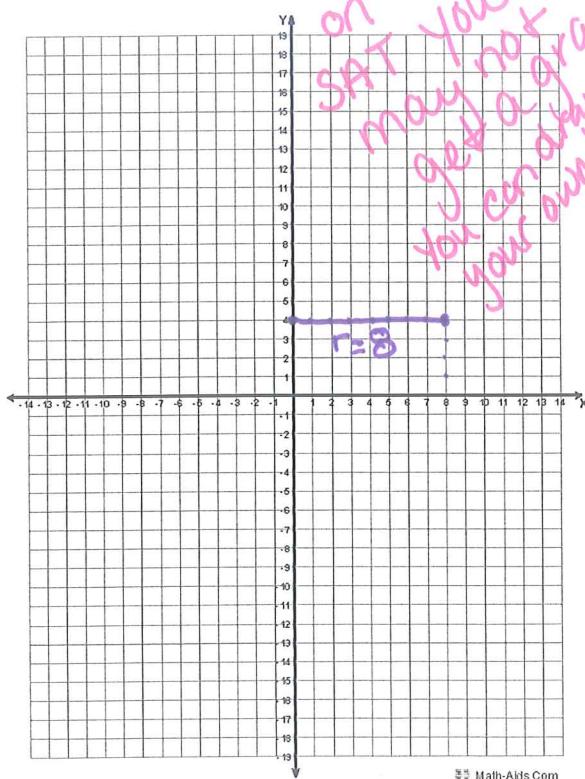
$$r = \sqrt{4}$$

$r = 2$

$$r = \sqrt{16}$$

$r = 4$

Ex 7. Write the equation of a circle with the center at (8, 4) and a radius with the endpoint (0, 4).



Find radius (AKA distance)  
distance is easy for  
this question because  
we just count...

$$r = 8$$

$$(x - h)^2 + (y - k)^2 = r^2$$

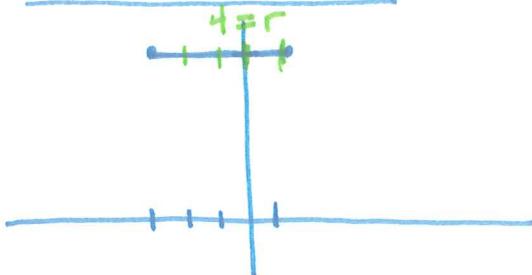
$$(x - 8)^2 + (y - 4)^2 = 8^2$$

$$(x - 8)^2 + (y - 4)^2 = 64$$

*h, k*

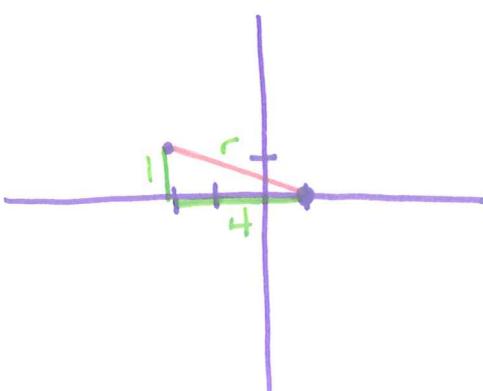
Ex 8. Write the equation of a circle with the center at  $(-3, 9)$  and a radius with the endpoint  $(1, 9)$ . (In Alg. 2, SAT, and exams you may not be given graph paper)

Find distance



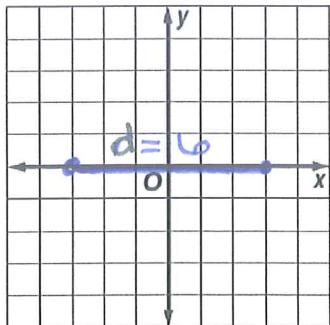
$$\begin{aligned} (x - -3)^2 + (y - 9)^2 &= 4^2 \\ (x + 3)^2 + (y - 9)^2 &= 16 \end{aligned}$$

Ex 9. Write the equation of a circle with the center at  $(-2, 1)$  and a radius with the endpoint  $(1, 0)$ . (In Alg. 2, SAT, and exams you may not be given graph paper)



$$\begin{aligned} 1^2 + 4^2 &= r^2 \\ 1 + 16 &\div r^2 \\ \sqrt{17} &= r \end{aligned} \quad \begin{aligned} (x - -2)^2 + (y - 1)^2 &= \sqrt{17}^2 \\ (x + 2)^2 + (y - 1)^2 &= 17 \end{aligned}$$

Ex 10. Write the equation of a circle whose diameter has endpoints  $(-3, 0)$  and  $(3, 0)$ .



$$d = 6 \div 2 \quad r = 3$$

Now find center: midpoint  $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$

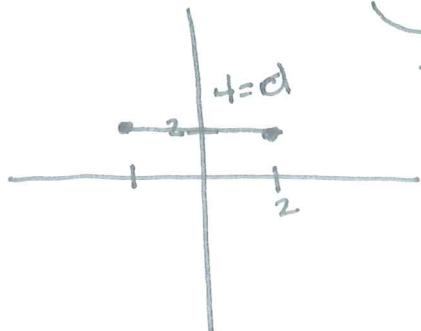
$$\left(\frac{-3+3}{2}, \frac{0+0}{2}\right) = \left(\frac{0}{2}, \frac{0}{2}\right) = (0, 0)$$

center:  $(0, 0)$

$$(x - 0)^2 + (y - 0)^2 = 3^2$$

$$x^2 + y^2 = 9$$

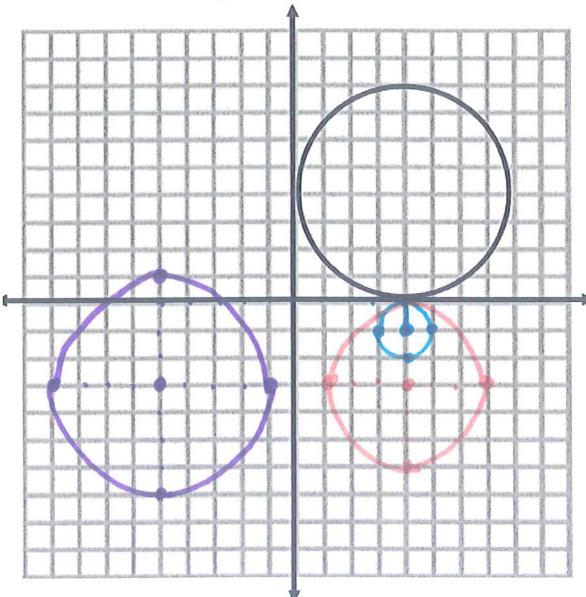
Ex 11. Write the equation of a circle whose diameter has endpoints  $(2, 2)$  and  $(-2, 2)$ .



$$\begin{aligned} d &= 4 & r &= 2 & x_1, y_1 & x_2, y_2 \\ \div 2 & & & & & \\ \text{Find midpoint} & & & & & \\ \left(\frac{2+(-2)}{2}, \frac{2+2}{2}\right) &= \left(\frac{0}{2}, \frac{4}{2}\right) & & & & \\ \text{Center: } (0, 2) & & & & & \boxed{r = 2} \\ (x - 0)^2 + (y - 2)^2 &= 2^2 \\ x^2 + (y - 2)^2 &= 4 \end{aligned}$$

Ex 12. The circle below is graphed from the equation  $(x - 4)^2 + (y - 4)^2 = 16$ .

- Graph and write an equation of another circle which is tangent to the one given. *W/ Shoulder partners define tangent.*
- Graph and write an equation of a third circle which is NOT tangent to the circle given, nor the circle from part a, and has a center at the origin.



a.) Center  $(4, -1)$   $r=1$

$$(x-4)^2 + (y+1)^2 = 1^2$$

$$\boxed{(x-4)^2 + (y+1)^2 = 1}$$

another example.

Center:  $(4, -3)$   $r=3$

$$(x-4)^2 + (y+3)^2 = 3^2$$

b.) Center  $(-5, -3)$   $r=4$

$$(x+5)^2 + (y+3)^2 = 4^2$$

$$\boxed{(x+5)^2 + (y+3)^2 = 16}$$

Ex 13. The 2 circles  $(x + 5)^2 + (y + 5)^2 = 25$  and  $(x - 5)^2 + (y - 5)^2 = 25$  are graphed in the standard  $(x, y)$  coordinate plane below. Which of the following circles, when graphed, will be tangent to both circles.

- I.  $x^2 + y^2 = 1$  *nope*  
 II.  $x^2 + y^2 = 100$  *nope*  
 III.  $\underline{(x-5)^2 + (y+5)^2 = 25}$  *tangent to both!*

- A. I only  
 B. III only  
 C. I and III only  
 D. I, II, and III

