

Write a two-column proof for each of the following.

1. Theorem: If two angles are supplementary to the same angle then they are congruent.

Given: $\angle 3$ and $\angle 4$ are supplementary; $\angle 3$ and $\angle 5$ are supplementary

Prove: $\angle 4 \cong \angle 5$

1.) $\angle 3$ and $\angle 4$ are Suppl.
 $\angle 3$ and $\angle 5$ are Suppl.

2.) $\angle 3 + \angle 4 = 180^\circ$
 $\angle 3 + \angle 5 = 180^\circ$

3.) $\angle 3 + \angle 4 = \angle 3 + \angle 5$

4.) $\angle 4 \cong \angle 5$

1. given

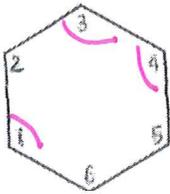
2.) def of suppl.

3.) substitution

4.) subtraction

2. Given: $m\angle 3 = 120^\circ$; $\angle 1 \cong \angle 4$; $\angle 3 \cong \angle 4$

Prove: $m\angle 1 = 120^\circ$



1. $\angle 3 = 120^\circ$
 $\angle 1 \cong \angle 4$
 $\angle 3 \cong \angle 4$

2.) $\angle 1 \cong \angle 3$

3.) $\angle 1 = 120^\circ$

1. given

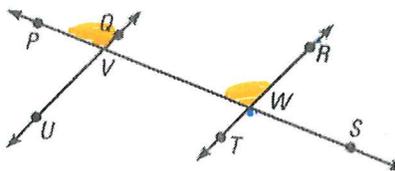
2.) transitive or Substitution

3.) transitive or Substitution

Write a two column proof for the following.

3. Given: $\angle QVW$ and $\angle RWV$ are supplementary

Prove: $\angle QVP \cong \angle RWV$



1. $\angle QVW$ and $\angle RWV$ are suppl.

2. $\angle QVW + \angle RWV = 180^\circ$

3.) $\angle QVW + \angle QVP = 180^\circ$

4.) $\angle QVW + \angle RWV = \angle QVW + \angle QVP$
- $\angle QVW$ - $\angle QVW$

5.) $\angle RWV \cong \angle QVP$

1. given

2. def of suppl.

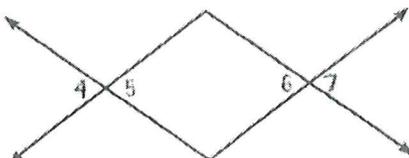
3.) Linear Pairs are Suppl.

4.) substitution

5.) subtraction

4. Given: $\angle 5 \cong \angle 6$

Prove: $\angle 4 \cong \angle 7$



1. $\angle 5 \cong \angle 6$

2.) $\angle 4 \cong \angle 5$
 $\angle 6 \cong \angle 7$

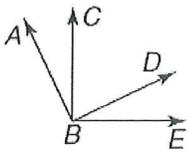
3.) $\angle 4 \cong \angle 7$

1. given

2.) Vertical \angle s are \cong
NOT def of

3.) substitution

5. Given: $\angle ABC$ and $\angle CBD$ are complementary.
 $\angle DBE$ and $\angle CBD$ form a right angle.
 Prove: $\angle ABC \cong \angle DBE$



1. $\angle ABC$ and $\angle CBD$ are compl
 $\angle DBE$ and $\angle CBD$ are compl.

1. given

2. $\angle ABC + \angle CBD = 90^\circ$
 $\angle DBE + \angle CBD = 90^\circ$

2. def of compl

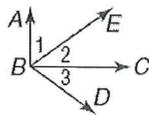
3. $\angle ABC + \angle CBD = \angle DBE + \angle CBD$

3. substitution

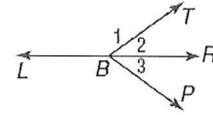
4. $\angle ABC \cong \angle DBE$

4. subtraction

6. Given: $\overline{AB} \perp \overline{BC}$;
 $\angle 1$ and $\angle 3$ are complementary.
 Prove: $\angle 2 \cong \angle 3$



7. Given: $\angle 1$ and $\angle 2$ form a linear pair.
 $m\angle 1 + m\angle 3 = 180$
 Prove: $\angle 2 \cong \angle 3$



Statements	Reasons
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a. $\overline{AB} \perp \overline{BC}$	a. given
b. $\angle ABC$ is a right angle	b. Definition of \perp
c. $m\angle ABC = 90$	c. Def. of right angle
d. $m\angle ABC = m\angle 1 + m\angle 2$	d. angle addition
e. $90 = m\angle 1 + m\angle 2$	e. Substitution
f. $\angle 1$ and $\angle 2$ are compl.	f. def of compl.
g. $\angle 1$ and $\angle 3$ are compl.	g. Given
h. $\angle 2 \cong \angle 3$	h. \angle s compl to the same \angle or $\cong \angle$ s are congruent

1.) $\angle 1$ and $\angle 2$ form a linear pair
 $\angle 1 + \angle 3 = 180^\circ$

1.) given

2.) $\angle 1 + \angle 2 = 180$

2.) linear pairs are suppl.

3.) $\angle 1 + \angle 3 = \angle 1 + \angle 2$

3.) substitution

4.) $\angle 3 \cong \angle 2$

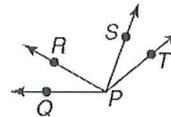
4.) subtraction

8. Copy and complete the following proof.

Given: $\angle QPS \cong \angle TPR$

Prove: $\angle QPR \cong \angle TPS$

Proof:



Statements	Reasons
a. $\angle QPS \cong \angle TPR$	a. Given
b. $m\angle QPS = m\angle TPR$	b. def of \cong
c. $m\angle QPS = m\angle QPR + m\angle RPS$ $m\angle TPR = m\angle TPS + m\angle RPS$	c. \angle addition
d. $\angle QPR + \angle RPS = \angle TPS + \angle RPS$	d. Substitution
e. $m\angle QPR = m\angle TPS$	e. subtraction
f. $\angle QPR \cong \angle TPS$	f. def of \cong