

Acc Geometry

Surface Area of Pyramids - Notes

Key

Prior to lesson:

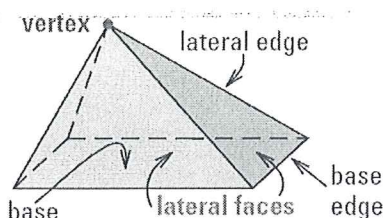
Pages: 1-4 Cut out and find the area

<http://www.misd.net/mathematics/ImplementingGeometryUnits/3Dimensional/Netspyramidsandprisms.pdf>

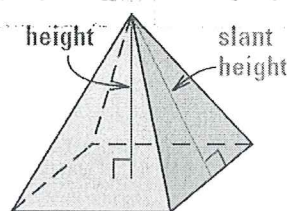
Put all work on the work sheet:

<http://www.misd.net/mathematics/ImplementingGeometryUnits/3Dimensional/pyramids.pdf>

A **pyramid** is a polyhedron in which the *base* is a polygon and the *lateral faces* are triangles with a common *vertex*. The intersection of two lateral faces is a *lateral edge*. The intersection of the base and a lateral face is a *base edge*. The *altitude*, or *height*, of the pyramid is the perpendicular distance between the base and the vertex.



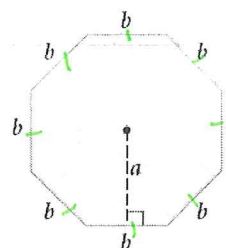
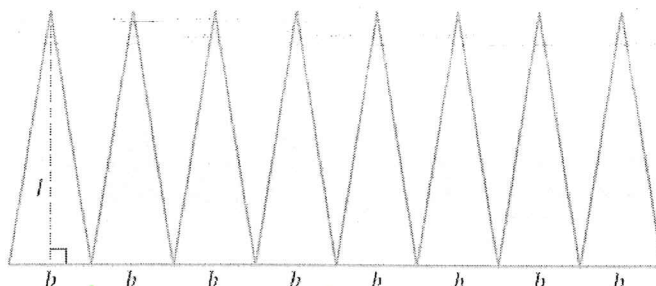
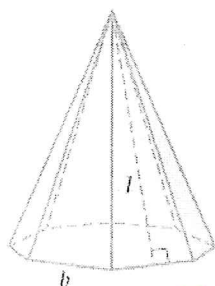
Pyramid



Regular pyramid

A **regular pyramid** has a regular polygon for a base and its height meets the base at its center. The *slant height* of a regular pyramid is the altitude of any lateral face. A nonregular pyramid does not have a slant height.

Write the expression for the lateral area and surface area of the regular pyramid.



$$SA = 8 \frac{1}{2} b \times a + 8 \frac{1}{2} b \cdot l$$

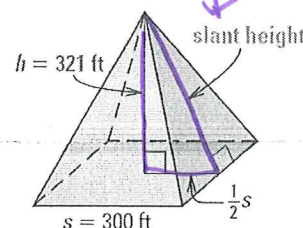
$$LA = 8 \frac{1}{2} b \cdot l$$

Find the lateral area and surface area of each solid. Round to the nearest tenth if necessary.

Example 1:



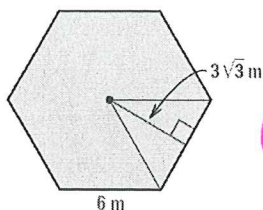
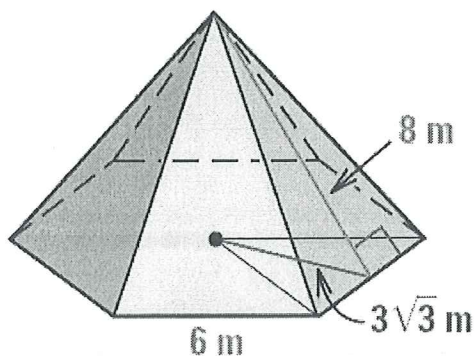
ARCHITECTURE The lateral faces of the Pyramid Arena in Memphis, Tennessee, are covered with steel panels. Use the diagram of the arena at the right to find the area of each lateral face of this regular pyramid.



one
one Lateral face = $\frac{1}{2} 300 \times 354.3$
 $A = 53145 \text{ ft}^2$

321
 $l = 354.3$
must find
150

Example 2:



It would be logical to use $\frac{1}{2}$ a P. or $6 \frac{1}{2} (6 \times 3\sqrt{3})$

$$SA = 6 \frac{1}{2} 6 \times 3\sqrt{3} = \text{Base}$$

$$6 \left(\frac{1}{2} 6 \times 8 \right)$$

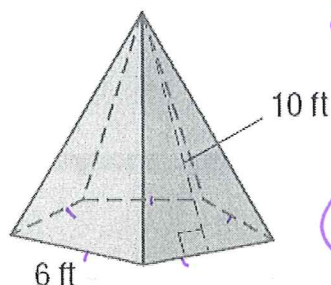
$$SA \approx 237.5 \text{ m}^2$$

$$SA = 6 \frac{1}{2} 6 \times 8$$

$$LA = 144 \text{ m}^2$$

Example 3:

Given: slant



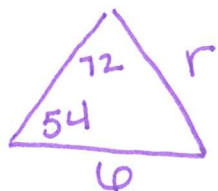
$$SA = 5 \frac{1}{2} 5.1^2 \sin 72$$

$$+ 5 \left(\frac{1}{2} 6 \times 10 \right)$$

$$SA = 211.8 \text{ ft}^2$$

$$SA = 5 \left(\frac{1}{2} 6 \times 10 \right)$$

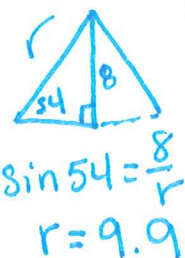
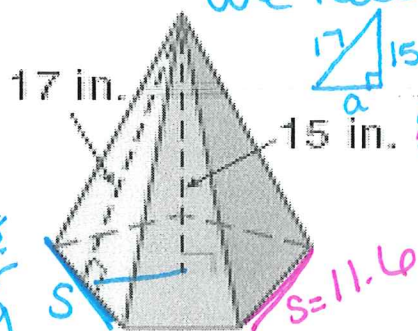
$$SA = 150 \text{ ft}^2$$



$$\frac{\sin 72}{6} = \frac{\sin 54}{r}$$

$$r \approx 5.1 \text{ ft}$$

Example 5: height + slant we need to find apothem



$$\sin 54 = \frac{8}{r}$$

$$r = 9.9$$



$$a = 8 \text{ in}$$

Find Side

$$\tan 54 = \frac{8}{x}$$

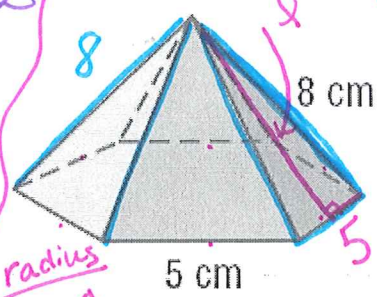
$$x = 5.8 \times 2$$

$$SA = 5 \frac{1}{2} 9.9^2 \sin 72$$

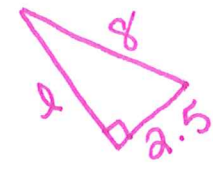
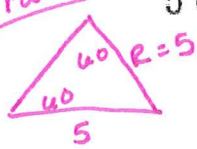
$$+ 5 \frac{1}{2} (11.6)(17)$$

$$SA = 726.0 \text{ in}^2$$

Example 4: Given Edge!



Find slant height



$$l = 7.6 \text{ cm}$$

$$SA = 6 \frac{1}{2} 5 \times 5 \sin 60$$

$$+ 6 \frac{1}{2} 5 \times 7.6$$

$$SA = 178.95 = 179.0 \text{ cm}^2$$