

Name: _____

Segment Relationships: Class Work1. Find the measure of \overline{BC} if B is the midpoint of \overline{AC} .

$$AB = BC \quad \text{def of midpt}$$

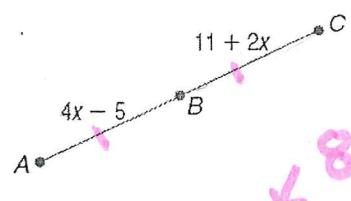
$$4x - 5 = 11 + 2x \quad \text{Substitution}$$

$$\begin{array}{r} -2x \\ \hline 2x - 5 = 11 \end{array}$$

$$\begin{array}{r} +5 +5 \\ \hline 2x = 16 \end{array} \quad \text{Subtraction}$$

$$\begin{array}{r} \frac{2}{2} \\ x = 8 \end{array} \quad \text{addition}$$

$$\begin{array}{r} \frac{2}{2} \\ x = 8 \end{array} \quad \text{division}$$



$$\begin{aligned} BC &= 11 + 2x \\ BC &= 11 + 2 \cdot 8 \\ BC &= 27 \end{aligned}$$

Find the value of the variable and ST if S is between R and T. Justify your steps.

2. $RS = 7a, ST = 12a, RT = 76$

$$RS + ST = RT$$

$$7a + 12a = 76$$

$$19a = 76$$

$$\begin{array}{|l} a = 4 \\ ST = 12 \cdot a \end{array}$$

$$ST = 12 \cdot 4$$

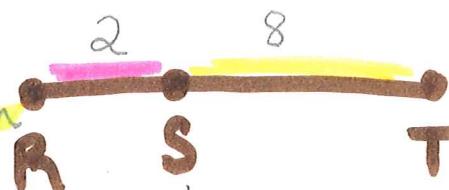
Segment addition

Substitution

CLT - Substitution

division

$$ST = 48$$



$$\begin{aligned} RS + ST &= RT \\ 2 + 8 &= 10 \end{aligned}$$

3. $RS = 12, ST = 2x, RT = 34$

$$RS + ST = RT$$

$$12 + 2x = 34$$

$$\begin{array}{|l} 2x = 22 \\ \hline x = 11 \end{array}$$

$$ST = 2(11)$$

Segment addition

Substitution

Subtraction

division

$$ST = 22$$

4. $RS = 4y - 1, ST = 2y - 1, RT = 5y$

$$RS + ST = RT$$

$$4y - 1 + 2y - 1 = 5y$$

$$\begin{array}{r} 6y - 2 = 5y \\ -6y \quad -6y \end{array}$$

$$\begin{array}{r} -2 = -1y \\ \hline 1 = 1y \end{array}$$

$$\begin{array}{|l} 1 \\ 2 = y \end{array}$$

Segment addition

Substitution

CLT -

Subtraction

division

$$\begin{aligned} ST &= 2y - 1 \\ ST &= 2 \cdot 2 - 1 \\ ST &= 3 \end{aligned}$$

Name: _____

Find the value of the variable and BC if B is between A and C. Justify your steps.

5. $AB = 6x, BC = 2x, AC = 96$

$$\begin{aligned} AB + BC &= AC && \text{Segment addition} \\ 6x + 2x &= 96 && \text{Substitution} \\ 8x &= 96 && \text{CLT} \\ x &= 12 && \text{division} \\ BC &= 24 \end{aligned}$$



6. $AB = 21, BC = 3a, AC = 36$

$$\begin{aligned} AB + BC &= AC && \text{Segment addition} \\ 21 + 3a &= 36 && \text{Substitution} \\ 3a &= 15 && \text{subtraction} \\ a &= 5 && \text{division} \\ BC &= 15 \end{aligned}$$

7. $AB = 6y + 2, BC = 2y - 6, AC = 3y$

$$\begin{aligned} AB + BC &= AC \\ 6y + 2 + 2y - 6 &= 3y \\ 8y - 4 &= 3y \\ -4 &= -5y \end{aligned}$$

$$\frac{4}{5} = y$$

$$, 8 = y \quad \text{or}$$

Segment addition
Substitution
CLT rule
Subtraction
division

$$B = 2 \times 8 - 6$$

$$BC = 2 \cdot \frac{4}{5} - 6$$

$$BC = \frac{-22}{5} \quad \text{or} \quad -4.4$$