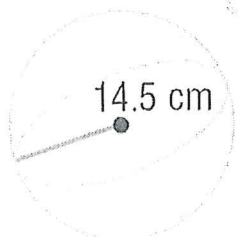


Basic Surface Area and Volume of Spheres Homework

Directions: Find the surface area and volume of each solid.
Round to the nearest tenth, if necessary.

1.



$$SA = 4\pi(14.5)^2$$

$$= 841\pi$$

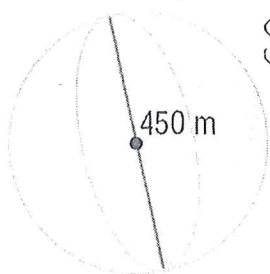
$$SA \approx 2642.1 \text{ cm}^2$$

$$V = \frac{4}{3}\pi(14.5)^3$$

$$SA = \underline{2642.1 \text{ cm}^2}$$

$$V = \underline{12770.1 \text{ cm}^3}$$

2.



$$r = 225 \text{ m}$$

$$SA = 4\pi(225)^2$$

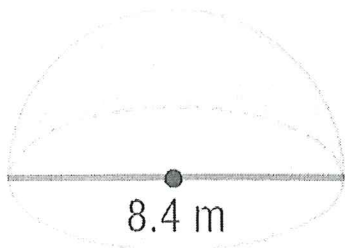
$$V = \frac{4}{3}\pi(225)^3$$

$$SA = \underline{636172.5 \text{ m}^2}$$

$$V = \underline{15187500 \text{ m}^3}$$

$$47712938 \text{ m}^3$$

3.



$$r = 4.2 \text{ m}$$

$$SA = \frac{1}{2}(4\pi(4.2)^2) + \pi(4.2)^2$$

$$= 35.28\pi + 17.64\pi$$

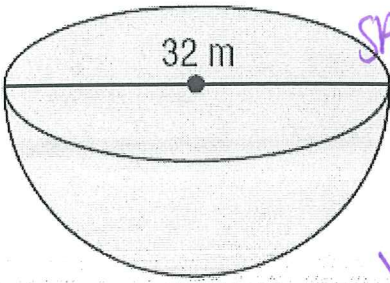
$$SA = \underline{166.3 \text{ m}^2}$$

$$V = \frac{1}{2}\left(\frac{4}{3}\pi(4.2)^3\right)$$

$$= 49.4\pi$$

$$V = \underline{155.2 \text{ m}^3}$$

4.



$$SA = \frac{1}{2} 4\pi(16)^2 + \pi 16^2$$

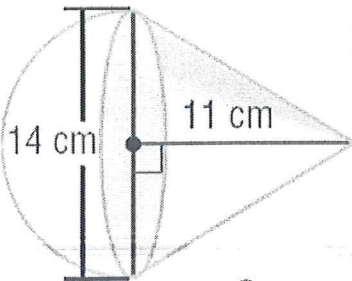
$$SA = 2412.7 m^2$$

$$SA = \underline{2412.7 m^2}$$

$$V = \frac{1}{2} \left(\frac{4}{3} \pi 16^3 \right)$$

$$V = \underline{8578.6 m^3}$$

5.



$$SA = \frac{1}{2} 4\pi 7^2 + \pi 7 \times 13$$

$$\underline{593.8 cm^2}$$

$$SA = \underline{593.8 cm^2}$$

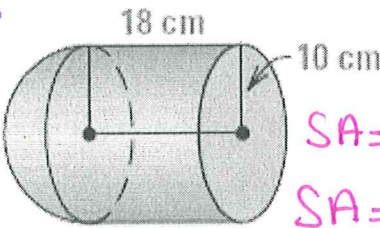
$$V = \underline{1282.8 cm^3}$$

$$r = 7$$

$$l = 13.0 cm$$

$$h = 11$$

6.



$$SA = Cyl - \pi r^2 + \frac{1}{2} sph \text{ no circle}$$

$$SA = \underline{2073.5 cm^2}$$

$$SA = \pi r^2 + 2\pi r h + \frac{1}{2} 4\pi r^2$$

$$SA = \pi 10^2 + 2\pi 10 \times 18 + \frac{1}{2} 4\pi 10^2$$

$$\underline{SA = 2073.5 cm^2}$$

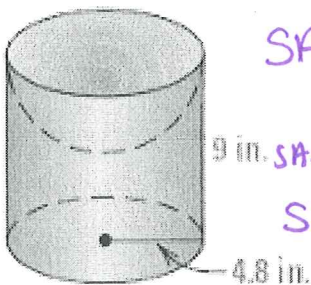
$$V = \underline{7749.3 cm^3}$$

$$V = \frac{1}{2} \frac{4}{3} \pi r^3 + \pi r^2 \times h$$

$$V =$$

$$V = \frac{1}{2} \left(\frac{4}{3} \pi 10^3 \right) + \pi 10^2 \times 18$$

7.



$$SA = \text{inside } \frac{1}{2} \text{ sphere} + \text{Cylinder} - \text{circle}$$

$$SA = \underline{488.6 in^2}$$

$$SA = \frac{1}{2} 4\pi r^2 + \pi r^2 + 2\pi r h$$

$$SA = \frac{1}{2} 4\pi 4.8^2 + \pi 4.8^2 + 2\pi 4.8 \times 9$$

$$V = \underline{419.8 in^3}$$

$$SA = 488.6$$

$$V = B \cdot h - \frac{1}{2} \frac{4}{3} \pi r^3$$

$$V = \pi 4.8^2 \cdot 9 - \frac{1}{2} \frac{4}{3} \pi \cdot 4.8^3$$

12-6

Study Guide and Intervention (continued)

Surface Areas of Spheres

Surface Areas of Spheres You can think of the surface area of a sphere as the total area of all of the nonoverlapping strips it would take to cover the sphere. If r is the radius of the sphere, then the area of a great circle of the sphere is πr^2 . The total surface area of the sphere is four times the area of a great circle.



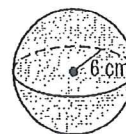
Surface Area
of a Sphere

If a sphere has a surface area of T square units and a radius of r units, then $T = 4\pi r^2$.

Example

Find the surface area of a sphere to the nearest tenth if the radius of the sphere is 6 centimeters.

$$\begin{aligned} T &= 4\pi r^2 && \text{Surface area of a sphere} \\ &= 4\pi \cdot 6^2 && r = 6 \\ &\approx 452.4 && \text{Simplify.} \end{aligned}$$



The surface area is 452.4 square centimeters.

Exercises

Find the surface area of each sphere with the given radius or diameter to the nearest tenth.

1. $r = 8$ cm

$$SA = 804.2 \text{ cm}^2$$

2. $r = 2\sqrt{2}$ ft

$$100.5 \text{ ft}^2$$

3. $r = \pi$ cm

$$SA = 124.0 \text{ cm}^2$$

4. $d = 10$ in.

$$SA = 314.2 \text{ in}^2$$

5. $d = 6\pi$ m

$$SA = 1116.2 \text{ m}^2$$

6. $d = 16$ yd

$$SA = 804.2 \text{ yd}^2$$

7. Find the surface area of a hemisphere with radius 12 centimeters.

$$SA = 1357.2 \text{ cm}^2$$

8. Find the surface area of a hemisphere with diameter π centimeters.

$$SA = 23.3 \text{ cm}^2$$

9. Find the radius of a sphere if the surface area of a hemisphere is 192π square centimeters.

$$SA = 192\pi \quad \boxed{r = 8 \text{ cm}}$$

Practice

Surface Area and Volume of Spheres

Find the surface area and volume of each sphere described below. Round to the nearest tenth.

1. The diameter is 100 centimeters.

$$r = 50$$

$$SA = 31415.9 \text{ cm}^2$$

$$V = \frac{4}{3} \pi 50^2$$

$$V = 523598.8 \text{ cm}^3$$

2. A great circle has a circumference 83.92 meters.

$$83.92 = 2\pi r \quad r = 13.4$$

$$SA = 4\pi(13.4)^2$$

$$SA = 226.98 \text{ m}^2$$

$$V = \frac{4}{3} \pi (13.4)^3$$

$$V = 10078.7 \text{ m}^3$$

3. The radius is 12 inches long.

$$SA = 1809.6 \text{ in}^2$$

$$V = 7238.2 \text{ in}^3$$

4. A great circle has an area of 70.58 square feet.

$$\frac{70.58}{\pi} = \frac{\pi r^2}{\pi}$$

$$r = 4.7$$

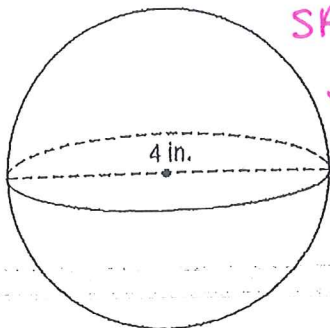
$$SA = 277.6 \text{ ft}^2$$

$$\sqrt{22.9663} = r$$

$$V = 92.5 \text{ ft}^3$$

Find the surface area and volume of each solid. Round to the nearest tenth.

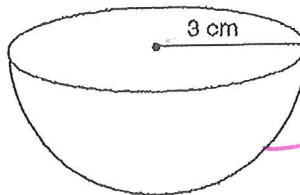
5.



$$SA = 50.3 \text{ in}^2$$

$$V = 33.5 \text{ in}^3$$

6.



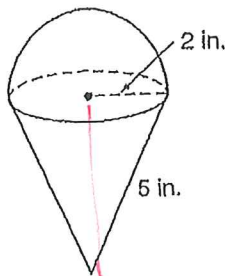
$$SA = \pi 3^2$$

$$+ \frac{1}{2} 4\pi 3^2$$

$$SA = 84.8 \text{ cm}^2$$

$$V = 56.5 \text{ cm}^3$$

7.



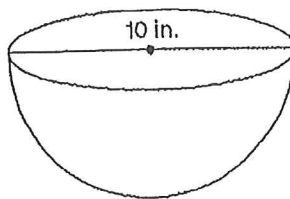
$$SA = \frac{1}{2} 4\pi r^2 + \pi r l$$

$$SA = \frac{1}{2} 4\pi 2^2 + \pi 2 \times 5$$

$$SA = 56.5 \text{ in}^2$$

LA of cone

8.



$$SA = \pi 5^2$$

$$+ \frac{1}{2} 4\pi 5^2$$

$$SA = 235.6 \text{ in}^2$$

$$V = 261.8 \text{ in}^3$$

$$V = \frac{1}{2} \left(\frac{4}{3} \pi r^3 \right) + \frac{1}{3} \pi r^2 \cdot h$$