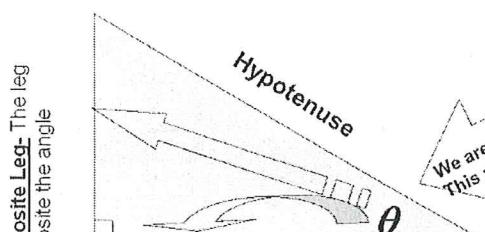


Acc Geometry Student Notes

Trigonometry

*Key
Make sure your calculator mode is set to degree!!*

Trig ratios work for RIGHT TRIANGLES only (for right now)



Opposite Leg - The leg opposite the angle

Hypotenuse - The side opposite the right angle

Adjacent Leg - The leg next to the angle

USING TRIG RATIOS

$$\sin \theta = \frac{\text{Length of leg opposite } \angle \theta}{\text{Length of hypotenuse}} = \frac{\text{Opposite}}{\text{Hypotenuse}}$$

$$\cos \theta = \frac{\text{Length of leg adjacent } \angle \theta}{\text{Length of hypotenuse}} = \frac{\text{Adjacent}}{\text{Hypotenuse}}$$

$$\tan \theta = \frac{\text{Length of leg opposite } \angle \theta}{\text{Length of leg adjacent } \angle \theta} = \frac{\text{Opposite}}{\text{Adjacent}}$$

Soh-Cah-Toa

- $\sin = \frac{O}{H}$
- $\cos = \frac{A}{H}$
- $\tan = \frac{O}{A}$

Some Old Hags

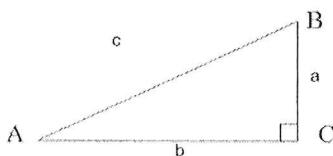


Can't Always Handle



Their Old Age

Consider the triangle ABC, shown below.



If our triangle has the measures of the side lengths labeled, we can express these ratios as fractions or decimals.

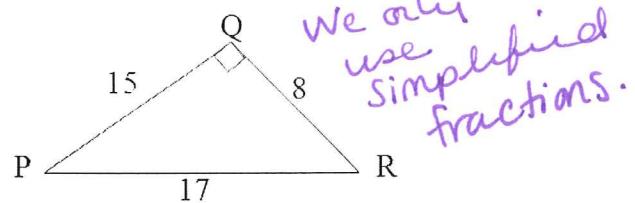
$$\sin \angle A = \frac{a/c}{a/b}$$

$$\tan \angle A = \frac{a/b}{b/a}$$

$$\sin \angle B = \frac{b/c}{b/a}$$

$$\tan \angle B = \frac{b/a}{a/b}$$

We do not use the right angle for trig ratios, so there is no sine, cosine, or tangent of $\angle C$.



$$\sin \angle P = \frac{8/17}{15/17}$$

$$\cos \angle P = \frac{15/17}{8/17}$$

$$\tan \angle P = \frac{8/17}{15/17}$$

$$\sin \angle R = \frac{15/17}{8/17}$$

$$\cos \angle R = \frac{8/17}{15/17}$$

$$\tan \angle R = \frac{15/8}{8/17}$$

Using your calculator with Trig:

$$\sin(57^\circ) = .84 \quad \cos(41^\circ) = .75$$

$$\theta = \tan^{-1}\left(\frac{5}{6}\right)$$

$$\theta = \sin^{-1}\left(\frac{9}{17}\right)$$

$$\theta \approx 39.8^\circ$$

$$\theta \approx 31.97^\circ$$

$$\sin(47^\circ) = \frac{x}{9}$$

$$\tan(61^\circ) = \frac{9}{x}$$

$$x = 6.58$$

$$\frac{x \cdot \tan(61)}{\tan(61)} = 9$$

$$x = 4.99$$

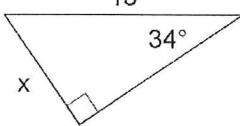
$$\tan \theta = \frac{20}{35} \quad \tan^{-1}(20/35) = \theta$$

$$\cos \theta = \frac{5}{7}$$

$$\theta = 29.74^\circ$$

Using Trigonometry to find Side Lengths

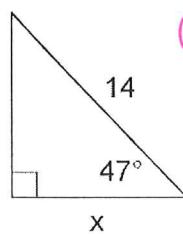
1.



$$\sin 34 = \frac{x}{13}$$

$$x = 7.27$$

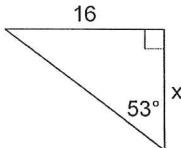
2.



$$\cos 47 = \frac{x}{14}$$

$$x = 9.55$$

3.

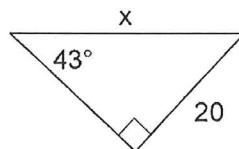


$$\tan 53 = \frac{16}{x}$$

$$x \cdot \tan 53 = \frac{16}{\tan 53}$$

$$x = 12.06$$

4.



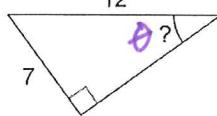
$$\sin 43 = \frac{x}{20}$$

$$x \sin 43 = 20$$

$$x = 29.33$$

Using Trigonometry to find Angles

1.

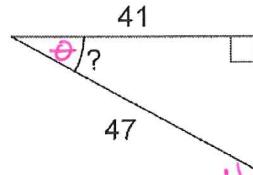


$$\sin \theta = \frac{7}{12}$$

$$\theta = \sin^{-1}(7/12)$$

$$\theta = 35.69^\circ$$

2.

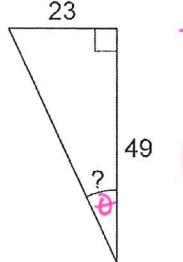


$$\cos \theta = \frac{41}{47}$$

$$\theta = \cos^{-1}(41/47)$$

$$\theta = 29.27^\circ$$

3.



$$\tan \theta = \frac{23}{49}$$

$$\theta = \tan^{-1}(23/49)$$

$$\theta \approx 25.14^\circ$$