

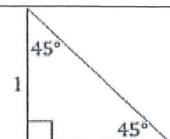
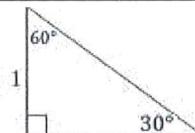
EXACT VALUES

Name _____

Hour _____

NO CALCULATOR ON THIS ENTIRE WORKSHEET

Use special right triangles to write the missing side lengths on each triangle.



Use the triangles above to state the EXACT VALUE of the trig functions WITHOUT using a calculator.

1. $\sin \frac{\pi}{6}$	2. $\cos \frac{\pi}{3}$	3. $\tan 60^\circ$	4. $\sin 45^\circ$	5. $\cos \frac{\pi}{4}$	6. $\tan \frac{\pi}{6}$	7. $\tan 45^\circ$
8. $\cos 30^\circ$	9. $\sin \frac{\pi}{3}$	10. $\cos 30^\circ$	11. $\sin \frac{\pi}{3}$	12. $\tan 30^\circ$	13. $\cos 45^\circ$	14. $\tan \frac{\pi}{4}$

Label the UNIT CIRCLE to help state the QUADRANTAL EXACT VALUES.

15. $\cos 90^\circ$	16. $\sin \frac{\pi}{2}$	17. $\cos \pi$	18. $\sin 2\pi$	
19. $\cos \frac{3\pi}{2}$	20. $\cos 0$	21. $\sin 180^\circ$	22. $\sin(-90^\circ)$	
23. $\sin 6\pi$	24. $\cos 9\pi$	25. $\tan \frac{\pi}{2}$	26. $\tan 2\pi$	
30. $\sin 180^\circ$	31. $\cos(-270^\circ)$	32. $\tan \frac{3\pi}{2}$	33. $\sin 2\pi$	
37. $\sin \theta > 0$ and $\cos \theta < 0$ (positive) (negative)	38. $\sin \theta < 0$ and $\cos \theta > 0$	39. $\sin \theta < 0$ and $\tan \theta > 0$	40. $\sec \theta > 0$ and $\csc \theta > 0$	skip

Name each QUADRANT described. (I, II, III, IV)

37. $\sin \theta > 0$ and $\cos \theta < 0$ (positive) (negative)	38. $\sin \theta < 0$ and $\cos \theta > 0$	39. $\sin \theta < 0$ and $\tan \theta > 0$	40. $\sec \theta > 0$ and $\csc \theta > 0$
			skip

State the EXACT VALUE WITHOUT using a calculator. Leave answers in simplest radical form or state that the value is undefined.

41. $\cos \frac{3\pi}{4}$

42. $\sin 210^\circ$

43. $\cos \frac{11\pi}{6}$

44. $\tan 120^\circ$

45. $\sin \frac{5\pi}{3}$

46. $\tan \frac{4\pi}{3}$

47. $\tan \frac{5\pi}{4}$

48. $\sin 225^\circ$

49. $\tan 300^\circ$

50. $\tan \frac{7\pi}{4}$

51. $\tan 150^\circ$

52. $\cos \left(-\frac{5\pi}{6} \right)$

53. $\sin \frac{5\pi}{6}$

54. $\sin(-120^\circ)$

55. $\cos 240^\circ$

56. $\tan \frac{7\pi}{6}$

57. $\cos \frac{2\pi}{3}$

58. $\cos(-45^\circ)$

59. $\sin(-240^\circ)$

60. $\sin 135^\circ$

61. $\tan 135^\circ$

62. $\cos 150^\circ$

63. $\sin 315^\circ$

64. $\cos 300^\circ$

65. $\tan 330^\circ$

66. $\cos 225^\circ$

67. $\sin \left(-\frac{\pi}{6} \right)$

68. $\sin \frac{7\pi}{2}$

69. $\cos \frac{5\pi}{2}$

70. $\tan 5\pi$

71. $\tan(-240^\circ)$

72. $\tan(-120^\circ)$

73. $\tan 135^\circ$

74. $\tan 150^\circ$

75. $\tan \frac{7\pi}{6}$

76. $\tan \frac{5\pi}{4}$

77. $\tan 315^\circ$

78. $\sin 300^\circ$

79. $\cos(-30^\circ)$

80. $\cos \pi$

81. $\sin \pi$

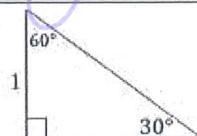
82. $\sin \frac{\pi}{2}$

EXACT VALUES

Name Key Hour _____

NO CALCULATOR ON THIS ENTIRE WORKSHEET

Use special right triangles to write the missing side lengths on each triangle.



Use the triangles above to state the EXACT VALUE of the trig functions WITHOUT using a calculator.

1. $\sin \frac{\pi}{6}$	2. $\cos \frac{\pi}{3}$	3. $\tan 60^\circ$	4. $\sin 45^\circ$	5. $\cos \frac{\pi}{4}$	6. $\tan \frac{\pi}{6}$	7. $\tan 45^\circ$
$\frac{1}{2}$	$\frac{1}{2}$	$\frac{\sqrt{3}}{2} = \frac{\sqrt{3} \cdot \sqrt{1}}{2}$ $\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1
8. $\cos 30^\circ$	9. $\sin \frac{\pi}{3}$	10. $\csc 30^\circ$	11. $\sec \frac{\pi}{3}$	12. $\sec 30^\circ$	13. $\csc 45^\circ$	14. $\cot \frac{\pi}{4}$
$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{\cos}{\sin} \frac{\sqrt{3}}{2}$	sin $\frac{\sqrt{3}}{2}$	tan $\sqrt{3}$	$\frac{\sqrt{2}}{2}$	$\tan 1$

Label the UNIT CIRCLE to help state the QUADRANTAL EXACT VALUES.

15. $\cos 90^\circ$	16. $\sin \frac{\pi}{2}$	17. $\cos \pi$	18. $\sin 2\pi$				
0	1	-1	0				
19. $\cos \frac{3\pi}{2}$	20. $\cos 0$	21. $\sin 180^\circ$	22. $\sin(-90^\circ)$				
0	1	0	-1				
23. $\sin 6\pi$	24. $\cos 9\pi$	25. $\tan \frac{\pi}{2}$	26. $\tan 2\pi$	27. $\tan 180^\circ$	28. $\sec 90^\circ$	29. $\csc 270^\circ$	
0	-1	undef.	0	0	\tan	\tan	
30. $\cot 180^\circ$	31. $\csc(-270^\circ)$	32. $\tan \frac{3\pi}{2}$	33. $\sec 2\pi$	34. $\sec \left(\frac{-\pi}{2}\right)$	35. $\cot \frac{\pi}{2}$	36. $\csc 7\pi$	
\cot 0	\csc 0	undef.	0	\tan	\tan	\tan	

Name each QUADRANT described. (I, II, III, IV)

37. $\sin \theta > 0$ and $\cos \theta < 0$ (positive) (negative)	38. $\sin \theta < 0$ and $\cos \theta > 0$	39. $\sin \theta < 0$ and $\tan \theta > 0$	40. $\sec \theta > 0$ and $\csc \theta > 0$
			skip

State the EXACT VALUE WITHOUT using a calculator. Leave answers in simplest radical form or state that the value is undefined.

41. $\cos \frac{3\pi}{4}$	42. $\sin 210^\circ$	43. $\cos \frac{11\pi}{6}$	44. $\tan 120^\circ$	45. $\sin \frac{5\pi}{3}$	46. $\tan \frac{4\pi}{3}$
$-\frac{\sqrt{2}}{2}$	$-\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$-\sqrt{3}$	$-\frac{\sqrt{3}}{2}$	$\sqrt{3}$
47. $\tan \frac{5\pi}{4}$	48. $\sin 225^\circ$	49. $\tan 300^\circ$	50. $\tan \frac{7\pi}{4}$	51. $\tan 150^\circ$	52. $\cos \left(\frac{-5\pi}{6}\right)$
1	$-\frac{\sqrt{2}}{2}$	$-\sqrt{3}$	-1	$\frac{\frac{1}{2}}{-\frac{\sqrt{3}}{2}} = -\frac{\sqrt{3}}{3}$	$-\frac{\sqrt{3}}{2}$
53. $\sin \frac{5\pi}{6}$	54. $\sin(-120^\circ)$ (240°)	55. $\cos 240^\circ$	56. $\tan \frac{7\pi}{6}$	57. $\cos \frac{2\pi}{3}$	58. $\cos(-45^\circ)$
$\frac{1}{2}$	$-\frac{\sqrt{3}}{2}$	$-\frac{1}{2}$	$\frac{-\frac{1}{2}}{-\frac{\sqrt{3}}{2}} = \frac{\sqrt{3}}{3}$	$-\frac{1}{2}$	$\frac{\sqrt{2}}{2}$
59. $\sin(-240^\circ)$ 120°	60. $\sin 135^\circ$	61. $\tan 135^\circ$	62. $\cos 150^\circ$	63. $\sin 315^\circ$	64. $\cos 300^\circ$
$\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{2}}{2}$	-1	$-\frac{\sqrt{3}}{2}$	$-\frac{\sqrt{2}}{2}$	$\frac{1}{2}$
65. $\tan 330^\circ$	66. $\cos 225^\circ$	67. $\sin\left(-\frac{\pi}{6}\right)$ $(^{\text{in } \text{Q}_4})$	68. $\sin \frac{7\pi}{2}$ $\frac{7\pi}{2} \Rightarrow \frac{3\pi}{2}$	69. $\cos \frac{5\pi}{2}$ $\frac{5\pi}{2} \Rightarrow 0$	70. $\tan 5\pi$
$\frac{-1}{\frac{\sqrt{3}}{2}} = -\frac{\sqrt{3}}{3}$	$-\frac{\sqrt{2}}{2}$	$-\frac{1}{2}$	-1	0	$\frac{0}{-1} = 0$

Now, try a few reciprocal functions. You may want to draw a labeled picture for these.

71. $\csc(-240^\circ)$ 120° tan $\frac{\sqrt{3}}{2} = -\sqrt{3}$ $-\frac{1}{2}$	72. $\sec(-120^\circ)$ (240°) tan $\sqrt{3}$	73. $\cot 135^\circ$ tan -1	74. $\sec 150^\circ$ tan $\frac{\frac{1}{2}}{-\frac{\sqrt{3}}{2}} = -\frac{\sqrt{3}}{3}$	75. $\cot \frac{7\pi}{6}$ tan $-\frac{1}{2} = \frac{\sqrt{3}}{3}$	76. $\csc \frac{5\pi}{4}$ tan 1
77. $\sec 315^\circ$ tan -1	78. $\cot 300^\circ$ sin $-\frac{\sqrt{3}}{2}$	79. $\csc(-30^\circ)$ cos $\frac{\sqrt{3}}{2}$	80. $\cot \pi$ cos -1	81. $\sec \pi$ sin 0	82. $\csc \frac{\pi}{2}$ sin 1